

• Intrinsic functions

Intrinsic (built in) functions are mathematical functions that you can use in your calculations (mostly)

- Commonly used intrinsic functions (see appendix B in the book for a complete list)

Transcendental functions

sqrt(x) → √x

exp(x) → e^x

log(x) → ln(x)

log10(x) → log₁₀(x)

cos(x), sin(x), tan(x) → Trig functions

acos(x), asin(x), atan(x) → inverse trig functions (principal angle)

atan2(y,x) → tan⁻¹(y/x) = 4 quadrant inverse tangent

sinh(x), cosh(x), tanh(x) → hyperbolic trig functions

- cos, sin, tan assume the input angle is in radians

- inverse trig functions return an angle in radians

- not defined for integer values

sin(1) will generate a compiler error

- The output type is the same as the input type

sin(1.0) = single precision sine

sin(1.0d0) = double precision sine

- If you need roots other than √, you need to use fractional exponents, but be careful

y = x^{1/3} → y = x**(1/3) is wrong (why?)

Several correct ways to do this

$$\begin{aligned}
y &= X^{**} (\text{DBLE}(1)/3) \\
&= X^{**} (1/\text{DBLE}(3)) \\
&= X^{**} (\text{DBLE}(1)/\text{DBLE}(3)) \\
&= X^{**} (1.0d0/3) \\
&= X^{**} (1/3.0d0) \\
&= X^{**} (1.0d0/3.0d0)
\end{aligned}$$

mixed mode with exponents.

- if you need an exponent of 3, use an integer 3

$$\begin{aligned}
y &= (\text{number})^{**} (\text{integer } 3) \\
&= (\text{number}) * (\text{number}) * (\text{number})
\end{aligned}$$

but

$$\begin{aligned}
y &= (\text{number})^{**} (\text{double } 3) \\
&= e^{\text{double } 3 * \ln(\text{number})}
\end{aligned}$$

more expensive, slightly less accurate

- so if you need

$$y = x^4$$

just use

$$y = x^{**} 4$$

- a negative number to a double power is undefined (unless you are using complex variables)

$$\begin{aligned}
y &= (-1.2d0)^{**} 4 \quad \longrightarrow \quad \text{OK} \\
y &= (-1.2d0)^{**} (1.0d0/3) = e^{\overbrace{(1.0d0/3) \cdot \ln(-1.2d0)}^{\text{undefined}}}
\end{aligned}$$

• other helpful functions

INT (x) → converts x to integer by dropping fractional part

DBLE(i) → promotes i to double

NINT(x) → rounds x to nearest integer

NINT (1.3) = 1

NINT (1.9) = 2

ABS(x) → absolute value

FLOOR(x) → round towards -∞

FLOOR (3.7) = 3

FLOOR (-3.7) = -4

CEILING(x) → rounds towards ∞

CEILING (3.7) = 4

CEILING (-3.7) = -3

MOD (x,y) → remainder when x is divided by y

MAX(a,b,c,...) → maximum of a,b,c,...

MIN(a,b,c,...) → minimum of a,b,c,...

output type is the same as the input type

NOTE: Angles are always assumed to be in radians unless explicitly given in degrees